

**THE GOLDEN RATIO, ATOMIC, IONIC AND
MOLECULAR CAPACITIES AND BONDING
DISTANCES IN HYDRIDES**

Raji Heyrovská

J. Heyrovský Institute of Physical Chemistry,
Academy of Sciences of the Czech Republic,
182 23 Prague 8, Czech Republic.
Raji.Heyrovská@jh-inst.cas.cz

It was shown¹ recently that the ground state energy of atomic hydrogen is also the electromagnetic energy of the *simplest atomic condenser* consisting of an electron (e⁻) and a proton (p⁺) separated by the Bohr radius, a_B,

$$eI_H = e^2/2\kappa a_B = (e^2/2\kappa)[(1/a_p) - (1/a_e)] \quad (1)$$

where I_H is the ionization potential, κ is the dielectric constant, a_B is divided into the Golden sections a_e and a_p at the point of charge neutrality, a_e = φa_p = a_B/φ and φ = φ² - 1 = (1 + 5^{1/2})/2 = 1.618 is the Golden ratio, κa_p = C_p, κa_e = C_e are capacities of e⁻ and p⁺ and κa_B = C_B is their Golden mean *atomic capacity*. See² for capacity-based low level hydrogen sensors.

For H as a *Golden ellipsoid*, with a_B as the major axis, the inter-focal distance = a_B/φ (= a_e).

The single bond distance between two atoms, d(AA) is³ twice the covalent radius d(A) *for any atom A* and is¹ the sum of the cationic radius d(A+) and anionic radius d(A-) as shown below,

$$d(AA) = d(A+) + d(A-) = \phi^2 d(A+) = \phi d(A-) \quad (2)$$

where φ divides d(AA) into the Golden sections d(A+) and d(A-) at the point of charge neutrality. The ionization potential I(AA) = e/2κd(AA) is given by (similar to eq. 1),

$$e/2\kappa d(AA) = (e/2\kappa)[1/d(A+) - 1/d(A-)] \quad (3)$$

where κd(A+) = C(A+) and κd(A-) = C(A-) are ionic capacities and κd(AA) = C(AA) is the Golden mean *molecular capacity* of AA (= A₂).

On the basis of eq. 2, the inter-ionic distances d(MX) of all alkali halides (MX) were explained¹ by the sums, d(M+) + d(X-), and hence no need for radius ratio corrections³.

Here, the 1:1 agreement of the calculated values d(AH),cal using the data^{3,4} for d(HH) and d(AA) for calculating the radii from eq. 2 with the observed^{3,4} distances d(AH),obs for about 40 hydrides (*storage materials for hydrogen*), is shown in the Table and Figure in the next column. Note that some partially ionic AH bonds (like hydrogen halides) are accounted for by an ionic and a covalent bond.

References:

1. R. Heyrovská, 35th Mtg. of DAMOP, APS, May 2004, Tucson, AZ, abs: P1.132 & P1.133.
2. <http://www.hydrogensafety.info/articles/04-feb-08.asp>
3. L. Pauling, *The Nature of the Chemical Bond*, Cornell Univ. Press, New York, 1960.
4. *CRC Handbook of C & P*, 1998 – 1999.

Table. Comparison of d(AH),obs,^{3,4} with d(AH),cal (in nm) for hydrides.

A	d(AA)/2 obs	d(AH), obs	d(AH),cal =	d(AH), cal
H	0.037	0.074	d(H+)+d(H-)	0.074
Li	0.175	0.160	d(A+)+d(H+)	0.161
Na	0.211	0.189	d(A+)+d(H+)	0.189
K	0.261	0.224	d(A+)+d(H+)	0.228
Rb	0.248	0.237	d(A+)+d(H-)	0.235
Cs	0.265	0.249	d(A+)+d(H-)	0.249
Be	0.114	0.134	d(A+)+d(H-)	0.133
Mg	0.161	0.173	d(A+)+d(H-)	0.169
Ca	0.198	0.200	d(A+)+d(H-)	0.197
Sr	0.243	0.215	d(A+)+d(H+)	0.213
Ba	0.251	0.223	d(A+)+d(H+)	0.220
Mn	0.133	0.173	d(A)+d(H)	0.170
Fe	0.144	0.148	d(A+)+d(H)	0.147
Co	0.126	0.154	d(A)+d(H+)	0.154
Ni	0.125	0.148	d(A)+d(H+)	0.153
Cu	0.128	0.146	d(A+)+d(H-)	0.144
Ag	0.144	0.162	d(A+)+d(H-)	0.156
Au	0.144	0.152	d(A+)+d(H-)	0.156
Zn	0.133	0.160	d(A)+d(H+)	0.161
Cd	0.149	0.176	d(A)+d(H+)	0.177
Hg	0.150	0.174	d(A)+d(H+)	0.178
B	0.089	0.119	d(A)+d(H+)	0.117
Al	0.143	0.165	d(A)+d(H+)	0.171
In	0.163	0.184	d(A)+d(H+)	0.191
Tl	0.194	0.187	d(A+)+d(H)	0.185
C	0.072	0.110	d(A)+d(H)	0.109
Si	0.118	0.148	d(A)+d(H+)	0.146
Ge	0.123	0.153	d(A)+d(H+)	0.151
Sn	0.151	0.179	d(A)+d(H+)	0.179
Pb	0.175	0.184	d(A+)+d(H-)	0.180
A	0.055	0.101	d(A-)+d(H)	0.105
P	0.109	0.142	d(A)+d(H)	0.146
As	0.122	0.152	d(A)+d(H+)	0.150
Sb	0.145	0.171	d(A)+d(H+)	0.173
O	0.060	0.096	d(A)+d(H)	0.097
S	0.094	0.134	d(A)+d(H)	0.131
Se	0.108	0.147	d(A)+d(H)	0.145
F	0.071	0.092	d(A+)+d(H)	0.091
Cl	0.099	0.127	d(A)+d(H+)	0.127
Br	0.115	0.142	d(A)+d(H+)	0.143
I	0.133	0.161	d(A)+d(H+)	0.161

